# National University of Lesotho MSc examinations EC6301 – Advanced Microeconomics I January 2023 100 Marks 3 Hours

**INSTRUCTION:** Answer **question one** and **any other two** questions.

### Question 1

Jeff likes both avocados and biscuits. The consumption bundle where Jeff consumes  $x_A$  (avocados) and  $x_B$  (biscuits) is written as  $(x_A, x_B)$ . You are given the following information

$$(10, 10) \sim (20, 5)$$
 and  $(9, 16) \sim (12, 12)$ 

We also know that Jeff's preferences are complete, transitive, continuous and strictly monotonic.

a) Discuss and show which of the following statements are true (if you have insufficient information state so):

i.	$(20,5) \gtrsim (9,16)$	[5]
ii.	(9, 16) > (18, 4)	[5]
iii.	$(20,5) \prec (9,15)$	[5]

b) You are now told that the set of consumption bundles (x<sub>A</sub>, x<sub>B</sub>) ∈ ℝ<sup>2</sup><sub>+</sub> which are on the same indifference curve as (20, 5) satisfy x<sub>B</sub> = 100/x<sub>A</sub>. Show that the set ≿ (20, 5) is defined by the relationship x<sub>B</sub> ≥ 100/x<sub>A</sub>. Does this information affect your previous conclusions?

[20]

- c) Discuss and show whether the set  $\geq$  (20, 5) is:
  - i. Closed [5]
  - ii. Convex [10]

#### Question 2

Assume a Bertrand duopoly with market demand  $Q = \alpha - \beta p$  in which firms have no fixed costs and identical marginal cost. Find a Bertrand equilibrium pair of prices,  $(p_1, p_2)$ , and quantities,  $(q_1, q_2)$ , when the following hold.

- a) Firm 1 has fixed costs F > 0. [7]
- **b**) Both firms have fixed costs F > 0. [9]
- c) Fixed costs are zero, but firm 1 has lower marginal cost than firm 2, so c<sub>2</sub> > c<sub>1</sub> > 0 (For this one assume the low-cost firm captures the entire market demand whenever the firms charge equal prices).

## **Question 3**

In an economy with two types of consumers, each type has the respective utility function and endowments:

$$u^{1}(x_{1}, x_{2}) = x_{1}x_{2}$$
 and  $e^{1} = (8, 2)$   
 $u^{2}(x_{1}, x_{2}) = x_{1}x_{2}$  and  $e^{2} = (2, 8)$ 

- *a*) Draw an Edgeworth box for this economy when there is one consumer of each type.
  - [5]
- *b*) Characterise as precisely as possible the set of allocations that are in the core of this twoconsumer economy. [7]
- c) Show that the allocation giving  $x^{11} = (4,4)$  and  $x^{21} = (6,6)$  is in the core. [3]
- d) Now replicate this economy once so that there are two consumers of each type, for a total of four consumers in the economy. Show that the double copy of the previous allocation, giving x<sup>11</sup> = x<sup>12</sup> = (4,4) and x<sup>21</sup> = x<sup>22</sup> = (6,6) is not in the core of the replicated economy. [10]

# Question 4

Consider the CES technology  $f(x_1, x_2) = (x_1^{\rho} + x_2^{\rho})^{\frac{1}{\rho}}$ .

- a) What is the elasticity of substitution of this technology? [5]
- b) Derive the cost function for this technology? [10]
- c) Verify, by using whatever duality results you think appropriate, that this cost function does indeed give rise to the underlying technology you began with. [10]